



# Sky-Pirates of the Stratosphere

Grade 10 math · Pythagorean theorem, Square roots, Exponents, Order of operations · Reading level grades 7-9

**Detective:** \_\_\_\_\_ **Date:** \_\_\_\_\_

A rogue airship pirate has stolen the legendary Golden Compass from the Sky Patrol academy. Only you can help trace the coordinates of the getaway vessel and unmask the culprit!

1. Solve each math problem. The answer is a number, and the letter beside it is what that number stands for.
2. In the clue boxes, write that letter in every box showing the same number, then read the secret clue.
3. Use each clue to cross suspects off the list. The one suspect left at the end is the culprit!

**My answer: the Sky Bandit is** \_\_\_\_\_

# Possible suspects

Cross off a row as each clue rules it out. The one left at the end is the culprit.

| NAME      | FLIGHT GEAR    | STOLEN GADGET | SIGNATURE PATCH      | HAIR STREAK COLOR   | TACTICAL WEAKNESS       |
|-----------|----------------|---------------|----------------------|---------------------|-------------------------|
| Kidd      | glider wings   | net launcher  | right shoulder patch | forest green streak | shrill dog whistles     |
| Drake     | rocket boots   | cloud bomb    | right shoulder patch | forest green streak | shrill dog whistles     |
| Bonnie    | glider wings   | laser cutter  | right shoulder patch | forest green streak | spicy chili snacks      |
| Morgan    | glider wings   | laser cutter  | right shoulder patch | forest green streak | dazzling bright flashes |
| James     | wind sail      | laser cutter  | right shoulder patch | neon blue streak    | spicy chili snacks      |
| Valentina | grappling hook | sonic whistle | left shoulder patch  | neon blue streak    | shrill dog whistles     |
| Buzz      | glider wings   | sonic whistle | left shoulder patch  | forest green streak | dazzling bright flashes |
| Bessie    | glider wings   | cloud bomb    | right shoulder patch | bright red streak   | shrill dog whistles     |
| Roger     | grappling hook | solar decoder | left shoulder patch  | forest green streak | spicy chili snacks      |
| Avery     | glider wings   | sonic whistle | left shoulder patch  | forest green streak | shrill dog whistles     |
| Alex      | wind sail      | cloud bomb    | left shoulder patch  | neon blue streak    | dazzling bright flashes |
| Steve     | wind sail      | laser cutter  | right shoulder patch | bright red streak   | dazzling bright flashes |
| Mae       | magnetic boots | solar decoder | right shoulder patch | forest green streak | shrill dog whistles     |
| Wendy     | glider wings   | cloud bomb    | right shoulder patch | forest green streak | spicy chili snacks      |
| Hook      | grappling hook | sonic whistle | right shoulder patch | forest green streak | dazzling bright flashes |
| Wilbur    | grappling hook | net launcher  | left shoulder patch  | neon blue streak    | dazzling bright flashes |
| Amelia    | glider wings   | laser cutter  | left shoulder patch  | neon blue streak    | shrill dog whistles     |
| Sally     | rocket boots   | sonic whistle | left shoulder patch  | bright red streak   | dazzling bright flashes |
| Charles   | magnetic boots | sonic whistle | right shoulder patch | forest green streak | shrill dog whistles     |
| Yuri      | glider wings   | laser cutter  | left shoulder patch  | forest green streak | dazzling bright flashes |
| Flint     | wind sail      | sonic whistle | right shoulder patch | forest green streak | shrill dog whistles     |

## CLUE 1

## Pythagorean theorem

Our patrol ship needs to calculate the shortest diagonal path between two floating docks to cut off the escape route.

Solve each problem, then write its letter in every clue box that shows the same number.

|    |    |    |    |    |     |    |    |    |    |     |    |    |    |    |    |    |    |
|----|----|----|----|----|-----|----|----|----|----|-----|----|----|----|----|----|----|----|
| T  |    |    | T  |    |     |    |    |    |    |     |    |    |    | T  |    |    |    |
| 85 | 10 | 26 | 85 | 10 | 100 | 26 | 58 | 65 | 20 | 26  | 82 | 15 | 20 | 85 | 13 | 82 | 26 |
| T  |    |    |    |    | T   |    |    |    |    |     |    |    |    |    |    |    |    |
| 85 | 10 | 26 | 15 | 26 | 85  | 87 | 40 | 13 | 15 | 111 | 10 | 26 | 29 |    |    |    |    |

legs 40 and 75, hypotenuse =  → **T**

legs 10 and 24, hypotenuse =  → **E**

legs 36 and 105, hypotenuse =  → **C**

legs 25 and 60, hypotenuse =  → **D**

legs 12 and 16, hypotenuse =  → **O**

legs 6 and 8, hypotenuse =  → **H**

legs 18 and 80, hypotenuse =  → **S**

legs 20 and 21, hypotenuse =  → **R**

legs 28 and 96, hypotenuse =  → **I**

legs 60 and 63, hypotenuse =  → **L**

legs 40 and 42, hypotenuse =  → **F**

legs 9 and 12, hypotenuse =  → **N**

legs 24 and 32, hypotenuse =  → **A**

legs 5 and 12, hypotenuse =  → **U**

Scratch space:

## CLUE 2 Square roots

The thief left a locked cargo crate with a square grid lock, and we must find the side length from its total area.

Solve each problem, then write its letter in every clue box that shows the same number.

|    |   |    |   |    |    |   |    |    |    |    |    |   |    |   |    |    |   |    |
|----|---|----|---|----|----|---|----|----|----|----|----|---|----|---|----|----|---|----|
| T  |   |    |   |    | T  |   |    |    |    |    |    |   |    |   |    |    | T |    |
| 17 | 4 | 10 | 5 | 14 | 17 | 2 | 10 | 12 | 12 | 12 | 16 | 5 | 16 | 7 | 14 | 24 | 4 | 17 |

  

|    |   |    |    |    |   |    |   |    |    |    |    |   |
|----|---|----|----|----|---|----|---|----|----|----|----|---|
|    |   |    |    |    |   |    |   |    |    | T  |    |   |
| 12 | 4 | 20 | 25 | 11 | 8 | 10 | 7 | 19 | 16 | 17 | 15 | 4 |

$\sqrt{289} = \square \rightarrow \text{[T]}$

$\sqrt{361} = \square \rightarrow \text{[P]}$

$\sqrt{121} = \square \rightarrow \text{[L]}$

$\sqrt{625} = \square \rightarrow \text{[U]}$

$\sqrt{144} = \square \rightarrow \text{[S]}$

$\sqrt{196} = \square \rightarrow \text{[I]}$

$\sqrt{64} = \square \rightarrow \text{[D]}$

$\sqrt{25} = \square \rightarrow \text{[W]}$

$\sqrt{256} = \square \rightarrow \text{[A]}$

$\sqrt{49} = \square \rightarrow \text{[R]}$

$\sqrt{4} = \square \rightarrow \text{[N]}$

$\sqrt{100} = \square \rightarrow \text{[E]}$

$\sqrt{576} = \square \rightarrow \text{[G]}$

$\sqrt{16} = \square \rightarrow \text{[H]}$

$\sqrt{400} = \square \rightarrow \text{[O]}$

$\sqrt{225} = \square \rightarrow \text{[C]}$

Scratch space:

## CLUE 3

A distress beacon is multiplying its signal strength at an exponential rate, and we need to determine its final power output.

Solve each problem, then write its letter in every clue box that shows the same number.

Diagram illustrating the iterative merging of sorted arrays into a single sorted array:

- Initial arrays (Size 4):  $[16, 196, 512, 243]$ ,  $[243, 196, 225]$ ,  $[100, 484, 27, 289, 343, 16, 49, 289]$ ,  $[100, 27, 16, 16]$
- Merged arrays (Size 8):  $[289, 343, 196, 400]$ ,  $[343, 484, 49]$ ,  $[128, 64, 27, 144, 27, 216, 729, 16]$
- Final array (Size 16):  $[289, 343, 196, 400, 343, 484, 49, 128, 64, 27, 144, 27, 216, 729, 16, 16]$

$4^2 = \square \rightarrow \boxed{\text{L}}$

$$3^6 = \boxed{\phantom{000}} \rightarrow \boxed{\text{A}}$$

$$20^2 = \boxed{\phantom{00}} \rightarrow \boxed{\text{P}}$$

$$22^2 = \boxed{\phantom{00}} \rightarrow \boxed{\text{H}}$$

$4^3 = \boxed{\phantom{000}} \rightarrow \boxed{\text{R}}$

$$8^3 = \boxed{\phantom{000}} \rightarrow \boxed{\text{U}}$$

$12^2 = \square \rightarrow \boxed{\text{M}}$

$$14^2 = \boxed{\phantom{00}} \rightarrow \boxed{0}$$

$7^3 = \boxed{\phantom{000}} \rightarrow \boxed{\text{T}}$

$15^2 = \boxed{\phantom{000}} \rightarrow \boxed{\text{G}}$

$7^2 = \boxed{\phantom{00}} \rightarrow \boxed{\text{E}}$

$$6^3 = \boxed{\phantom{000}} \rightarrow \boxed{\text{N}}$$

$3^3 = \square \rightarrow \square$

$10^2 = \boxed{\phantom{00}} \rightarrow \boxed{\text{W}}$

$$17^2 = \boxed{\phantom{000}} \rightarrow \boxed{S}$$

$3^5 = \square \rightarrow \boxed{\text{D}}$

$2^7 = \square \rightarrow \boxed{\text{C}}$

Scratch space:

## CLUE 4 Order of operations

To bypass the airship's encrypted firewall, we must solve a multi-step equation in the exact mathematical sequence.

Solve each problem, then write its letter in every clue box that shows the same number.

|     |    |    |    |    |     |     |    |    |    |    |    |    |    |    |    |    |     |    |    |
|-----|----|----|----|----|-----|-----|----|----|----|----|----|----|----|----|----|----|-----|----|----|
| T   |    |    |    |    |     |     |    |    |    |    |    |    |    |    |    |    |     |    |    |
| 106 | 64 | 68 | 70 | 55 | 14  | 119 | 68 | 11 | 98 | 87 | 69 | 38 | 70 | 38 |    |    |     |    |    |
|     |    |    |    |    | T   |     |    |    |    |    |    |    |    |    |    |    |     |    |    |
| 82  | 55 | 87 | 68 | 70 | 106 | 100 | 87 | 68 | 68 | 11 | 64 | 38 | 98 | 87 | 82 | 98 | 103 | 68 | 87 |

|                                            |                                            |                                             |
|--------------------------------------------|--------------------------------------------|---------------------------------------------|
| $43 + 9 \times 7 = \square \rightarrow$ T  | $11 \times 9 - 1 = \square \rightarrow$ I  | $11 \times 12 - 29 = \square \rightarrow$ B |
| $3 \times 8 - 10 = \square \rightarrow$ U  | $12 \times 5 - 5 = \square \rightarrow$ O  | $7 \times 12 - 14 = \square \rightarrow$ S  |
| $8 \times 10 - 11 = \square \rightarrow$ W | $12 \times 9 - 8 = \square \rightarrow$ G  | $40 + 7 \times 4 = \square \rightarrow$ E   |
| $1 + 2 \times 5 = \square \rightarrow$ N   | $12 \times 10 - 1 = \square \rightarrow$ V | $76 + 3 \times 2 = \square \rightarrow$ F   |
| $12 \times 7 - 20 = \square \rightarrow$ H | $14 + 8 \times 3 = \square \rightarrow$ A  | $78 + 3 \times 3 = \square \rightarrow$ R   |

Scratch space:

## CLUE 5 Square roots - the last clue

We need to analyze the perfect square dimensions of the landing pad where the getaway vessel temporarily docked.

First solve each problem. Then find each answer in the numbered list below and cross that sentence out. One sentence will be left - that is exactly what the villain did!

### Step 1 - solve these:

$\text{sqrt}(49) = \boxed{\phantom{00}}$

$\text{sqrt}(121) = \boxed{\phantom{00}}$

$\text{sqrt}(1) = \boxed{\phantom{00}}$

$\text{sqrt}(64) = \boxed{\phantom{00}}$

$\text{sqrt}(100) = \boxed{\phantom{00}}$

$\text{sqrt}(16) = \boxed{\phantom{00}}$

$\text{sqrt}(36) = \boxed{\phantom{00}}$

$\text{sqrt}(9) = \boxed{\phantom{00}}$

$\text{sqrt}(144) = \boxed{\phantom{00}}$

$\text{sqrt}(81) = \boxed{\phantom{00}}$

$\text{sqrt}(4) = \boxed{\phantom{00}}$

### Step 2 - cross out the sentence with each answer:

1. The villain caught the thermal draft, then shattered the alarm glass with a sonic whistle.
2. The villain swung through the rigging, then shattered the alarm glass with a sonic whistle.
3. The villain blasted past the guard towers, then snared the guarding falcons with a net launcher.
4. The villain swung through the rigging, then unlocked the secure safe with a solar decoder.
5. The villain blasted past the guard towers, then blinded the security cameras with a cloud bomb.
6. The villain caught the thermal draft, then snared the guarding falcons with a net launcher.
7. The villain scaled the metallic hull, then shattered the alarm glass with a sonic whistle.
8. The villain glided over the canyon, then sliced open the vault door with a laser cutter.
9. The villain caught the thermal draft, then unlocked the secure safe with a solar decoder.
10. The villain glided over the canyon, then shattered the alarm glass with a sonic whistle.
11. The villain scaled the metallic hull, then unlocked the secure safe with a solar decoder.
12. The villain scaled the metallic hull, then snared the guarding falcons with a net launcher.

# Answer Key

## Sky-Pirates of the Stratosphere

### Culprit: Drake

rocket boots · cloud bomb · right shoulder patch · forest green streak · shrill dog whistles

Trail: Start 21 → Clue 1 19 → Clue 2 11 → Clue 3 5 → Clue 4 4 → Clue 5 1

### Clue 1 (Pythagorean theorem): "THE THIEF DOES NOT USE THE NET LAUNCHER"

legs 40 and 75, hypotenuse = 85 (T) · legs 10 and 24, hypotenuse = 26 (E) · legs 36 and 105, hypotenuse = 111 (C) · legs 25 and 60, hypotenuse = 65 (D) · legs 12 and 16, hypotenuse = 20 (O) · legs 6 and 8, hypotenuse = 10 (H) · legs 18 and 80, hypotenuse = 82 (S) · legs 20 and 21, hypotenuse = 29 (R) · legs 28 and 96, hypotenuse = 100 (I) · legs 60 and 63, hypotenuse = 87 (L) · legs 40 and 42, hypotenuse = 58 (F) · legs 9 and 12, hypotenuse = 15 (N) · legs 24 and 32, hypotenuse = 40 (A) · legs 5 and 12, hypotenuse = 13 (U)

### Clue 2 (Square roots): "THE WITNESS SAW A RIGHT SHOULDER PATCH"

$\sqrt{289} = 17$  (T) ·  $\sqrt{361} = 19$  (P) ·  $\sqrt{121} = 11$  (L) ·  $\sqrt{625} = 25$  (U) ·  $\sqrt{144} = 12$  (S) ·  $\sqrt{196} = 14$  (I) ·  $\sqrt{64} = 8$  (D) ·  $\sqrt{25} = 5$  (W) ·  $\sqrt{256} = 16$  (A) ·  $\sqrt{49} = 7$  (R) ·  $\sqrt{4} = 2$  (N) ·  $\sqrt{100} = 10$  (E) ·  $\sqrt{576} = 24$  (G) ·  $\sqrt{16} = 4$  (H) ·  $\sqrt{400} = 20$  (O) ·  $\sqrt{225} = 15$  (C)

### Clue 3 (Exponents): "LOUD DOG WHISTLES WILL STOP THE CRIMINAL"

$4^2 = 16$  (L) ·  $3^6 = 729$  (A) ·  $20^2 = 400$  (P) ·  $22^2 = 484$  (H) ·  $4^3 = 64$  (R) ·  $8^3 = 512$  (U) ·  $12^2 = 144$  (M) ·  $14^2 = 196$  (O) ·  $7^3 = 343$  (T) ·  $15^2 = 225$  (G) ·  $7^2 = 49$  (E) ·  $6^3 = 216$  (N) ·  $3^3 = 27$  (I) ·  $10^2 = 100$  (W) ·  $17^2 = 289$  (S) ·  $3^5 = 243$  (D) ·  $2^7 = 128$  (C)

### Clue 4 (Order of operations): "THE SOUVENIR WAS A FOREST GREEN HAIR FIBER"

$43 + 9 \times 7 = 106$  (T) ·  $11 \times 9 - 1 = 98$  (I) ·  $11 \times 12 - 29 = 103$  (B) ·  $3 \times 8 - 10 = 14$  (U) ·  $12 \times 5 - 5 = 55$  (O) ·  $7 \times 12 - 14 = 70$  (S) ·  $8 \times 10 - 11 = 69$  (W) ·  $12 \times 9 - 8 = 100$  (G) ·  $40 + 7 \times 4 = 68$  (E) ·  $1 + 2 \times 5 = 11$  (N) ·  $12 \times 10 - 1 = 119$  (V) ·  $76 + 3 \times 2 = 82$  (F) ·  $12 \times 7 - 20 = 64$  (H) ·  $14 + 8 \times 3 = 38$  (A) ·  $78 + 3 \times 3 = 87$  (R)

### Clue 5 (Square roots): surviving statement is box 5 → Drake

$\sqrt{49} = 7$  ·  $\sqrt{121} = 11$  ·  $\sqrt{1} = 1$  ·  $\sqrt{64} = 8$  ·  $\sqrt{100} = 10$  ·  $\sqrt{16} = 4$  ·  $\sqrt{36} = 6$  ·  $\sqrt{9} = 3$  ·  $\sqrt{144} = 12$  ·  $\sqrt{81} = 9$  ·  $\sqrt{4} = 2$